## A heterogenitások hatásának vizsgálata energia hálózatokban mtaEC Géza Ódor and Bálint Hartmann Centre for Energy Research of the Hungarian Academy of Sciences



#### **Electric Energy & Power Network**



- Electric energy is critical for our technological civilization
- Purpose of electric power grid: generate/transmit/distribute
- Challenges: multiple scales, nonlinear, & complex system, growing number of renewables &



## Challenge: Scale-free blackout size distributions



Figure 4. Probability distribution function of energy unserved for North American blackouts 1993-1998.

Self-Organized Criticality (SOC) is assumed for modeling this:

Competition of supply and demand

B. Carreras et al, Proceedings of Hawaii International Conference on System Sciences, Jan. 4-7, 2000, Maui, Hawaii. 2000 IEEE

Extreme events occur more frequently than by Gaussian model prediction

US HV 4941 nodes

# Power-grids form heterogeneous, hierarchical modular networks

• Multi-level : high - medium - low voltages



#### Synthetic Power grid generation

- We created large: HV (transmission) MV (sub-transmission) - LV(distribution) level graphs with weights
- For HV : from utilities and system operators
- For MV, LV: representative or reference network models (RNM) : NEW algoritm using iterative random MATLAB processes, using empirical electrical distributions

#### Admittance matrix:

for HV: Hungarian example for MV,LV: synthetic grid modeling

HV: undirected loop top  $L = \frac{1}{N(N-1)} \sum_{j \neq i} d(i, j)$ 

$$C^{W} = \frac{1}{N} \sum_{i} 2n_{i}/k_{i}(k_{i}-1) d t C^{\Delta} = \frac{\text{number of closed triplets}}{\text{number of connected triplets}}$$
of nodes



FIG. 1: Structural representation of the synthetic networks. Left side: HV, right side: a radial subnetwork. The highlighted red node connects the two layers. The network on the picture has 68850 nodes and 68849 edges.

TABLE	I:	Power-grids	generated	and	studied.
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Network	Ν	Edge no.	L	$C^{\Delta}$	$C^W$
1M	1098583	1098601	$1.7440\times10^{6}$	0	0
1.5M	1455343	1455367	$1.0457\times 10^6$	0.0594	0.0486
2.5M	2356331	2356360	$1.6162\times 10^6$	0.0851	0.0586
23M	23551140	23551254	$2.1129\times 10^6$	0.0626	0.0741

#### Network graph analysis

#### • Basic network distributions:









Topological dimension: <*N(R)> ~ R<sup>D</sup>* by Breadth first search from each
 node

$$D_{\text{eff}}(D+1/2) = \frac{\ln\langle N_R \rangle - \ln\langle N_{R+1} \rangle}{\ln(R) - \ln(R+1)}$$



FIG. 4: Average number of nodes within chemical distance R in the 23 graph. Dashed line shows a power-law fit for 4 < R < 20. Inset: local slopes defined in Eq. 6.

#### The synchronization model

 Network failures, blackouts can be described by de-synchronization of AC power

Simplest model : second order Kuramoto equations for phases  $\theta_i$  of oscillatc  $\dot{\theta}_i(t) = \omega_i(t)$  $\dot{\omega}_i(t) = \omega_{i,0} - \alpha \dot{\theta}_i(t) + \frac{K}{N_i} \sum_{j \neq i} A_{ij} \sin[\theta_i(t) - \theta_j(t)]$ 

coupled by control parameter: K, admittance matrix:  $A_{ij}$  and  $\alpha$ : dissipation

Quenched disorder in the topology, admittances and in the intrinsic

#### The synchronization transition

Synchronization is measured by the order parameter

$$z(t_k) = r(t_k) \exp i\theta(t_k) = 1/N \sum_{j} \exp [i\theta_j(t_k)], \qquad R(t_k) = \langle r(t_k) \rangle$$
Numerical integration  
results in a first order  
phase transition for  
a fully coupled  
(mean-field) network

FIG. 2: Hysteresis in the steady state order parameter in fully coupled networks of sizes N = 1000 (boxes) and N = 500(diamonds). Inset:  $\sigma_R(K)$  peaks for the two different network sizes investigated.

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#### **Two-dimensional lattice grid**

- Synchronization transition on homogeneous, 2D lattices:
- Numerical integration
   results in a crossover to synchronization at large K values
- "Fast" relaxation to the steady state (no power-law)
- Hysteresis
- What is the consequenc of heterogeneities ?



**Figure 6.** Phase synchronization transition in the steady state in 2D networks of sizes  $N = 500 \times 500$  (red bullets),  $N = 1000 \times 1000$  (blue boxes) using a = 3 and  $N = 500 \times 500$  (green stars) using a = 1. Inset: time dependence or R(t), in case of the  $N = 500 \times 500$  lattice, for control parameters: K = 700, 350, 200, 150, 100, 80, 60, 50 in case of synchronized initial condition (top to bottom curves) and K = 700, 100 de-synchronized initial condition (top to bottom curves).

#### Heterogeneities in other network models

On lower dimensional regular, Euclidean lattices: critical point between ordered and disordered phases due to the fluctuations



Quenched disorder : Slowly decaying rare regions



Rounds phase transition, Griffiths phase:





#### Synchronization in power-grids

1.0

Synthetic and real power grids considered without noise

Bigger synchronization *R* values than in 2*D* at a given *K* but the stability is weak

Exponential relaxation remains

Adding noisy oscillators: small effects. Even for a Gaussian with  $\sigma = 3$ : few percent drop,

\* \* \* 0.8 0.6 Ы 0.4 ▲ 1M 0.2  $\nabla$ 2.5M ∇1M low ○ 500 x 500 \*US 0.0 50 100 150 Κ

Maximum -20% of R at the transition

#### Synchronization in power-grids

Standard deviation  $\sigma_R$  over 50 samples and fixed time windows in the steady state

Fluctuations peaks disappear as  $N \rightarrow \infty$ 

No real phase transition, but a crossover, like in the Kuramoto model

Crossover peaks are at lower *K-s (~30)* than in *2D (~100-200)* 



### De-synchronization avalanches in power grids

The duration distribution of de-synchronization events:

 $R = 1 \rightarrow R = 1/N^{0.5}$ 



**Figure 10.** Avalanche duration distribution in the 1M power grid for a = 3 and different coupling values K = 0.7, 0.6, 0.5, 0.4, 0.2 (top to bottom solid curves). Dashed lines: PL fits for the tails.

#### K-dependent power-law tails: scale-free distributions like in GP

#### **Centralized vs distributed sources**

Renewable energy sources  $\rightarrow$  distributed across the whole network  $\rightarrow$  Instability ?

We compared HV sources  $\leftrightarrow$  distributed



#### Conclusions

The topological heterogeneity smears the transition that remains for large couplings only : no real phase transition but a crossover

With respect to 2D topological+weight disorder enhances the synchronization but decreases the fluctuations

Scale-free desynchronization duration avalanches  $\rightarrow$  Rare large events occur more frequently than in case of a Gaussian mathematical model

Frustrated synchronization ?

K-dependent power-law tails : heterogeneity effects (no SOC assumption)

Fault tolerance study : many stochastic elements have low influence

## Distributed energy sources: After initial instability higher synchronization than in HV

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